

PHYS6011 Experimental Problem Set

Part II

1. Given an average luminosity of $50 \times 10^{30} \text{ cm}^{-2}\text{s}^{-1}$ estimate how often the following inclusive physics processes occur at CDF:

$$p\bar{p} \Rightarrow b\bar{b} : \sigma \sim 10 \text{ } \mu\text{b}$$

$$p\bar{p} \Rightarrow W : \sigma \sim 10 \text{ nb}$$

$$p\bar{p} \Rightarrow t\bar{t} : \sigma \sim 10 \text{ pb}$$

2. The top width (i.e. the quantum uncertainty in its mass) is expected to be about 1.5 GeV. What is its lifetime? Explain why there are no top-flavoured hadrons given $\Lambda_{QCD} \approx 200 \text{ MeV}$.
3. What fraction of top pair production events will have a “dilepton” final state, i.e.

$$p\bar{p} \rightarrow t\bar{t} \rightarrow l_1 l_2 \nu_1 \nu_2 b\bar{b}$$

where l_1 and l_2 can be either two electrons, two muons or one of each.

4. In a semileptonic top pair candidate event there is a muon, a transverse momentum imbalance, two b -tagged jets and two non-tagged jets. The measured jet energies and directions ($\theta = 0$ is the beam direction, the x axis is horizontal and all angles are in radians) are as follows:

$$b_1: \quad E = 145 \text{ GeV} \quad \theta = 0.3 \quad \phi = -1.6$$

$$b_2: \quad E = 90 \text{ GeV} \quad \theta = 1.3 \quad \phi = -0.2$$

$$j_1: \quad E = 125 \text{ GeV} \quad \theta = 0.9 \quad \phi = 2.1$$

$$j_2: \quad E = 15 \text{ GeV} \quad \theta = 1.7 \quad \phi = -1.7$$

- (a) The momenta of the jets approximates the momenta of the original partons. Write down the 4-momenta of the four final state quarks (assume j_1 and j_2 come from massless partons).

- (b) Show that the light quark jets are consistent with being the decay products of a W (Hint: assume they come from the decay $X \rightarrow j_1 j_2$ and calculate the mass of X).
 - (c) Which of the two b jets probably came from the same top quark as this hadronically decaying W ?
5. A search for the supersymmetric partner of the top quark, the stop or \tilde{t} , using 200 pb^{-1} has an expected background of 17 events with a total systematic error of 5 events. The data shows 30 selected events.
- (a) How significant is this excess?
 - (b) Assuming that this excess is really due to a signal, approximately how much more data will need to be collected before a discovery can be claimed? (Assume the systematic error remains constant).